

# CSC544 Assignment #1

due Thursday 2/12 in class

## Problems

1. Give the state diagrams of FAs recognizing the following languages (assume  $\Sigma = \{0, 1\}$ ):
  - (a)  $\{w \mid w \text{ begins with a 1 and ends with a 0}\}$
  - (b)  $\{w \mid w \text{ contains at least three 1s}\}$
  - (c)  $\{w \mid w \text{ does not contain the substring 110}\}$

2. Use the construction given in the proof of Theorem 1.45 (2nd edition), Theorem 1.22 (1st edition), Slide 14 of the slide set on NFAs,

<http://homepage.cs.uri.edu/faculty/hamel/courses/2015/spring2015/csc544/lecture-notes/03-regular-languages-NFA.pdf>

to give the state diagram of the NFA recognizing the union of the two languages described in Problem 1a and Problem 1b, respectively.

3. Prove that the language  $L = \{a^m b^n \mid a, b \in \Sigma \text{ and } m, n \geq 0\}$  is regular.
4. Prove that the language  $L' = \{a^m b^n \mid a, b \in \Sigma \text{ and } m \geq 0 \text{ and } n \geq m\}$  is not regular.